

Know the following identities:

- (1) Difference of Squares: $a^2 - b^2 = (a + b)(a - b)$
- (2) Difference of Cubes: $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$
- (3) Sum of Cubes: $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$
- (4) $(a + b)^2 = a^2 + 2ab + b^2$
- (5) $(a + b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$

1. Factor into linear factors whenever possible. Then solve.

- (a) $x^2 + 2x + 1 = 0$
 $(x + 1)^2 = 0 \implies x = -1$
- (b) $x^2 + 6x + 8 = 0$
 $(x + 2)(x + 4) = 0 \implies x = -2 \text{ or } x = -4$
- (c) $x^2 - 2x - 24 = 0$
 $(x - 6)(x + 4) = 0 \implies x = 6 \text{ or } x = -4$
- (d) $3x^2 + x - 2 = 0$
 $(x + 1)(3x - 2) = 0 \implies x = -1 \text{ or } x = 2/3$
- (e) $2x^2 + x - 3 = 0$
 $(x - 1)(2x + 3) = 0 \implies x = 1 \text{ or } x = -3/2$
- (f) $x^2 - 4 = 0$
 $(x + 2)(x - 2) = 0 \implies x = \pm 2$
- (g) $9x^2 - 16 = 0$
 $(3x + 4)(3x - 4) = 0 \implies x = \pm 4/3$
- (h) $x^3 + 8 = 0$
 $(x + 2)(x^2 - 2x + 4) = 0 \implies x = -2$
- (i) $x(x - 3) + 4x - 12 = 0$
 $x(x - 3) + 4(x - 3) = (x - 3)(x + 4) = 0 \implies x = 3 \text{ or } x = -4$

2. Solve.

- (a) $\frac{1}{x-3} = 2$
 $x = 7/2$
- (b) $\frac{2x-1}{2} + \frac{-1}{x-2} = 0$
 $x = 0 \text{ or } x = 5/2$
- (c) $\frac{1}{x+1} + \frac{2}{x-1} = -1$
 $x = 0 \text{ or } x = -3$