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Section: 11 12 13

1. Find the Taylor polynomial of order 2 for  $f(x) = \sqrt{x}$  centered at  $a = 4$ .

$$f(x) = x^{1/2} \quad f(4) = 4^{1/2} = 2$$

$$f'(x) = \frac{1}{2} x^{-1/2} \quad f'(4) = \frac{1}{2} \cdot 4^{-1/2} = \frac{1}{4}$$

$$f''(x) = -\frac{1}{4} x^{-3/2} \quad f''(4) = -\frac{1}{4} \cdot 4^{-3/2} \\ = -\frac{1}{4} \cdot \frac{1}{2^3} = -\frac{1}{32}$$

$$T_2(x) = f(4) + f'(4)(x-4) + \frac{f''(4)}{2!}(x-4)^2 \\ = 2 + \frac{1}{4}(x-4) + \frac{-1/32}{2!}(x-4)^2$$