## Math 242 Exam 2, Spring 2024

Name:

Section: 7 8

| Question | Points | Score |
|----------|--------|-------|
| 1        | 0      |       |
| 2        | 0      |       |
| 3        | 0      |       |
| 4        | 0      |       |
| 5        | 0      |       |
| 6        | 0      |       |
| Total:   | 0      |       |

- You have 75 minutes to complete this exam.
- Please ask if anything seems confusing or ambiguous.
- You must show all your work unless the problem states otherwise. You will get almost no credit for solutions that are not fully justified.
- You may not use notes or calculators on this exam.
- You do not need to simplify your answers.
- Good luck!

| Homework   |  |
|------------|--|
| Worksheets |  |
| Quizzes    |  |
| Exam 1     |  |
| Exam 2     |  |
| Total      |  |

1. Evaluate the following integrals.

(a) 
$$\int \frac{1}{\sqrt{4-x}} dx.$$

(b) 
$$\int \frac{1}{\sqrt{4-x^2}} dx$$
.

(c) 
$$\int \sqrt{4-x^2} \ dx.$$

(d) 
$$\int \frac{x}{\sqrt{4-x^2}} dx.$$

(e) 
$$\int \frac{1}{\sqrt{4-x^4}} dx$$
.

(f) 
$$\int \frac{1}{x\sqrt{4-x^2}} dx.$$

(g) 
$$\int \frac{\sqrt{4-x^2}}{x} dx.$$

(h) 
$$\int \frac{x^2}{\sqrt{4-x^2}} dx.$$

(i) 
$$\int \frac{1}{x\sqrt{x^2-4}} dx.$$

(j) 
$$\int \frac{1}{r^2 \sqrt{r^2 - 4}} dx$$
.

(k) 
$$\int \frac{1}{\sqrt{x^2 - 4}} dx.$$

(1) 
$$\int \frac{1}{\sqrt{x^2+4}} \, dx$$
.

(m) 
$$\int \frac{x^3}{\sqrt{x^2+4}} dx.$$

(n) 
$$\int \frac{1}{x^2 + 4} dx$$
.

(o) 
$$\int \frac{x}{x^2 + 4} dx.$$

(p) 
$$\int \frac{x^2}{x^2+4} dx$$
.

(q) 
$$\int \frac{x}{x^2 + 8x + 7} dx$$
.

(r) 
$$\int \frac{x+1}{x^2-4} dx$$
.

(s) 
$$\int \frac{x}{x^2 - 2x + 4} dx.$$

(t) 
$$\int \frac{3}{x^3 + 2x} \, dx.$$

(u) 
$$\int \cos^5(x) dx$$
.

(v) 
$$\int \sec^4 x \ dx$$
.

(w) 
$$\int \sin^2 x \cos^3 x \ dx.$$

(x) 
$$\int \cos^2 x \ dx$$
.

(y) 
$$\int \sin^4 x \ dx$$
.

(z) 
$$\int \cot^2 x \ dx$$
.

2. (a) 
$$\int \cot^3 x \csc^3 x \ dx.$$

(b) 
$$\int \tan^3 x \sec^3 x \ dx.$$

(c) 
$$\int \tan^4 x \sec^4 x \ dx.$$

(d) 
$$\int \sin(2x)\cos(3x) \ dx.$$

(e) 
$$\int \sin(2x)\sin(3x) \ dx.$$

(f) 
$$\int_{-1}^{1} \frac{1}{x} dx$$
.

(g) 
$$\int_0^\infty \frac{2x}{(1+x^2)^3} dx$$
.

(h) 
$$\int_0^1 \frac{1}{\sqrt{1-x^2}} dx$$
.

(i) 
$$\int_0^2 \frac{1}{(x-1)^{2/5}} dx$$
.

(j) 
$$\int_{1}^{\infty} \frac{\ln x}{x^3} dx.$$

(k) 
$$\int_0^\infty \frac{1}{x^2 + 4} \, dx$$
.

(1) 
$$\int_{3}^{\infty} \frac{1}{x^2 - 4} dx$$
.

(m) 
$$\int_{1}^{2} \frac{1}{x \ln x} dx$$
.

3. Give the abstract partial fration decomposition for

$$\frac{x^3 + x - 17}{x^3(x^2 + 7)^3(2x - 1)}$$

- 4. Approximate  $\int_{-2}^{2} x^3 dx$  using  $S_4$  and  $T_4$ .
- 5. For the following integrals find an n that guarantees that Simpson's Rule  $S_n$  is within and error of at most  $10^{-4}$ . Some useful absolute value properties are |ab| = |a||b| and  $|a+b| \le |a| + |b|$ . You do not have to simplify your answer.

(a) 
$$\int_0^1 x \cos(2x) \ dx$$
. You are given that  $\frac{d^4}{dx^4} x \cos(2x) = 16(2\sin(2x) + x\cos(2x))$ .

(b) 
$$\int_{-1}^{1} e^{-x^2} dx$$
. You are given that  $\frac{d^4}{dx^4} e^{-x^2} = 4e^{-x^2} (4x^2 - 12x^2 + 3)$ .

(c) 
$$\int_{-1}^{0} \frac{1}{1-x} dx$$
. You are given that  $\frac{d^4}{dx^4} \frac{1}{1-x} = \frac{24}{(1-x)^5}$ .

6. Find the limit of the following sequences.

(a) 
$$a_n = 3 + (0.1)^n$$

(b) 
$$a_n = \frac{2n+1}{1-\sqrt{n}}$$

(c) 
$$a_n = (-1)^n \left(1 - \frac{1}{n}\right)$$

(d) 
$$a_n = \sqrt{\frac{3n}{n+1}}$$

(e) 
$$a_n = \left(1 + \frac{9}{n}\right)^n$$

$$(f) a_n = \ln n - \ln(n+1)$$

(g) 
$$a_n = \sqrt[n]{n^4}$$

(h) 
$$a_n = \frac{n!}{5^n 6^n}$$

(i) 
$$a_n = \sum_{k=1}^n (-1)^n \frac{1}{2^n}$$

(j) 
$$a_n = 5^{1/n}$$

(k) 
$$a_n = (1.2)^n$$

(l) 
$$a_n = \frac{2^n}{2^n - 1}$$

(m) 
$$a_n = \frac{n!}{(n+2)!}$$

(n) 
$$a_n = \frac{4^n}{n!}$$