Math 242 Exam 3, Spring 2024

Name:

Section: 11 12 13

Question	Points	Score
1	0	
2	0	
3	0	
4	0	
5	0	
Total:	0	

- You have 50 minutes to complete this exam.
- Please ask if anything seems confusing or ambiguous.
- You must show all your work unless the problem states otherwise. You will get almost no credit for solutions that are not fully justified.
- You may not use notes or calculators on this exam.
- You do not need to simplify your answers.
- Good luck!

Homework	
Worksheets	
Quizzes	
Exam 1	
Exam 2	
Exam 3	
Total	

- (i) Sequences $\{a_n\}$ are infinite lists of numbers. Make sure you practice your limit techniques.
- (ii) Series $\sum_{n=1}^{\infty} a_n = a_1 + a_2 + a_3 + \cdots$ is the sum of a sequence. It is the limit of the sequence of *n*-th partial sums $s_n = a_1 + \cdots + a_n$.
- (iii) A sequence is **not** the same as a series

$$\sum_{n=1}^{\infty} a_n \neq \lim_{n \to \infty} a_n$$

1. Find the limit of the following sequences, otherwise state that sequence diverges.

(a)
$$\left\{\frac{2n^2}{3n^2 - 1}\right\}$$

(b)
$$\left\{\frac{\ln n + (-1)^n}{3n^2 - 1}\right\}$$

(c)
$$\left\{(-1)^{n+1}\frac{2n}{3n - 1}\right\}$$

(d)
$$\left\{\left(\frac{4}{5}\right)^n\right\}$$

(e)
$$\left\{\sqrt[n]{n}\right\}$$

2. Which of the following series converge, if the series converges find its sum.

(a)
$$\sum_{n=0}^{\infty} \frac{2^n}{5^n}$$

(b) $\sum_{n=1}^{\infty} \frac{9^{n-1}}{2^n}$
(c) $\sum_{n=1}^{\infty} \frac{2^n + 3^n}{7^n}$
(d) $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}2^n}{3^n}$
(e) $\sum_{n=1}^{\infty} \frac{1}{(n+1)(n+2)}$
(f) $\sum_{n=1}^{\infty} (\arctan(n+1) - \arctan(n+2))$

3. Determine which of the following series converge or diverge. Clearly state the tests you are using and give full reasoning.

4. Determine if the following series converge absolutely, converge conditionally, or if they diverge.

(a)
$$\sum_{n=3}^{\infty} \frac{1}{n \ln n}$$

(b)
$$\sum_{n=3}^{\infty} \frac{(-1)^n}{n \ln n}$$

(c)
$$\sum_{n=1}^{\infty} \frac{\cos(n^3)}{n^2 + \sqrt{n}}$$

(d)
$$\sum_{n=1}^{\infty} (-1)^n \frac{n^n}{n!}$$

(e)
$$\sum_{n=1}^{\infty} (-1)^{n-1} \frac{\ln}{n^3}$$

(f)
$$\sum_{n=1}^{\infty} \frac{(-1)^n}{\sqrt{n}}$$

5. Find the interval of convergence and radius of convergence for the following power series.

(a)
$$\sum_{n=1}^{\infty} (x+2)^n$$

(b) $\sum_{n=1}^{\infty} \frac{(2x+3)^n}{n}$
(c) $\sum_{n=1}^{\infty} (-1)^n \frac{x^n}{2^n n!}$
(d) $\sum_{n=1}^{\infty} n! (x-3)^n$
(e) $\sum_{n=1}^{\infty} \frac{x^n}{n \ln n}$
(f) $\sum_{n=1}^{\infty} \frac{nx^n}{2^n (n^2+1)}$
(g) $\sum_{n=1}^{\infty} \frac{(3x+1)^{2n+1}}{2n+2}$